# Energy balance of the house



#### Energy balance of the tokamak



Under the assumption of a simplified power balance, the heating power  $P_H$  is partially absorbed in the plasma and leads to an increase of the plasma energy  $W_p$  and the rest is lost as the loss power  $P_L$ 

$$P_H = \frac{dW_p}{dt} + P_L$$

The energy confinement time is defined as the characteristic time scale of the exponential decay of the plasma energy  $W_p$  due to the loss power  $P_L$ :

$$\tau_E = \frac{W_p}{P_L} = \frac{W_p}{P_H - dW_p/dt}$$

Choosing the quasistationary phase of the plasma discharge, where  $\frac{dW_p}{dt} = 0$  gives:

$$\tau_{E}(t) = \frac{W_{p}(t)}{P_{H}(t)}$$

On the GOLEM tokamak the only heating mechanism of the plasma is ohmic heating  $P_{OH}$  resulting from the plasma current  $I_p$  flowing in a conductor with finite resistivity  $R_p$ . The time dependence of the ohmic heating power can be calculated as:

$$P_H(t) = P_{OH}(t) = R_p(t) \cdot I_p^2(t)$$

The global plasma energy content  $W_p$  can be simply calculated from the temperature estimation  $T_e(0, t)$ , average density  $n_e$  and plasma volume  $V_p$ , based on the ideal gas law, taking into account the assumed

$${\mathcal T}_e(r,t)={\mathcal T}_e(0,t)\left(1-rac{r^2}{a^2}
ight)^2$$
 temperature profile:

$$W_p(t) = V_p \frac{n_e k_B T_e(0,t)}{3}.$$

The information that the magnetic field reduces the degrees of freedom of the particles to two has been used to derive this formula.

$$V_p \approx 80$$

The time evolution of the central electron temperature  $T_e(0, t)$  is calculated from equation based on Spitzer's resistivity formula (see eg. [Brotankova, J., 2009],[Wesson, 2004]):

$$T_{e}(0,t) = \left(\frac{R_{0}}{a^{2}} \frac{8Z_{eff.}}{1544} \frac{1}{R_{p}(t)}\right)^{2/3}, [eV; m, \Omega]$$

For particular case of the GOLEM tokamak it says:

$$T_e(0,t) = 0.9 \cdot \left(\frac{I_p(t)}{U_l(t)}\right)^{2/3}, [eV; A, V]$$

## Towards Electron energy confinement time $\tau_E$



## Towards Plasma current $I_p$



1) With some statistical effort. 2) Do it in the stationary phase, i.e. current constant, to avoid inductive phenomena. 3) 1 us step. 4) Rogowski Coil calibration constant =  $5.3 \cdot 10^6$  A/Vs 5) Uloop calibration constant = 5.5



#### Brotankova, J. (PhD. thesis 2009).

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#### Wesson, J. (Third Edition, 2004).

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